- 1. What is the tens digit (the digit second from the right) of 11^{2009} ? 9
- 2. What is the radius of the circle with equation $x^2 4x = 1 y^2 6y$? $\sqrt{14}$
- 3. How many vertices does a regular icosahedron have? 12

4.
$$\cos\left(2\sin^{-1}\frac{1}{5}\right) = \frac{23}{25}$$

- 5. Put the following mathematicians in order according to their year of birth, starting with the first born: Galois, Gauss, Hilbert, Newton. Newton, Gauss, Galois, Hilbert
- 6. Find a fourth-degree polynomial with real coefficients that has *i* and 2-i as roots. (Do not leave your answer in factored form.)

(many answers possible, one is $x^4 - 4x^3 + 6x^2 - 4x + 5$)

- 7. A triangle, M, is formed from \triangle ABC by constructing segments that connect the midpoints of the three sides. What is the ratio of the area of M to the area of \triangle ABC? 1/4
- 8. How many odd numbers are in the 17^{th} row of Pascal's triangle (where the 0^{th} row is **1** and the 1^{st} row is **1 1**)? 4
- 9. A Pythagorean triple (a, b, c) consists of three positive integers such that $a^2 + b^2 = c^2$. Write all Pythagorean triples that contain the number 37. (Consider triples in which *a* and *b* are interchanged to be equal, that is (3, 4, 5) and (4, 3, 5) are regarded as one triple.)

(12,35,37), (37,684,685)

10. A googol (in base ten) is 1 followed by one hundred zeros. Within ten, how many digits are there in a googol written in base five? Accept anything between 134 and 154