## 2018 Round One Qualifying Test for Who Wants to Be a Mathematician

1. Find the $y$-intercept ( $y$-coordinate only) of the line whose equation is $2 x+5 y=7$. $\qquad$
2. $2+4+6+8+\ldots+2018=$
(write your answer as a number, not a product)
3. $\left(\cos \frac{\pi}{12}+\sin \frac{\pi}{12}\right)\left(\cos \frac{\pi}{12}-\sin \frac{\pi}{12}\right)=$ (simplify so that your answer contains no trig functions)
4. What ancient Greek mathematician had a "sieve," used for finding prime numbers, named after him? (circle one)
a. Archimedes
b. Eratosthenes
c. Euclid
d. Pythagoras
5. Write $\frac{\log _{5} 9}{\log _{25} 3}$ as a rational number.
6. For which one of the following choices for $m$ are the base $m$ numbers $25_{m}$ and $27_{m}$ both primes? (circle one)
a. 8
b. 9 c. 11
d. 12
e. 13
7. You and two friends decide to pay a restaurant bill by having each person flip a fair, two-sided coin. If all three coins show heads or all show tails, you will split the bill three ways. Otherwise, the person whose coin landed differently from the other two will pay the entire bill. What is the probability that you will not have to pay anything?
8. Suppose that $m$ and $n$ are positive integers such that $5 m+3 n=41$. What is the smallest possible value for $\left|m^{2}-n^{2}\right|$ ?
9. In rectangle $A B C D$ at right, $D P$ is perpendicular to $P C$. Find $x$, the distance from $A$ to $P$, where $P$ is between $A$ and the midpoint of segment AB.
a. $3-2 \sqrt{2}$
b. $3-\sqrt{2}$
c. $3-\sqrt{7}$
d. $3-\sqrt{7} / 2$

10. What is the largest prime factor of $2^{14}+1$ ?
