## 2015 Qualifying Test Round One

1. Find the slope of the line whose equation is 2y - 3x = 5.

- 2. What is the fourth digit to the right of the decimal point in the decimal expansion of  $\pi$ ?
- 3. The *x*-coordinate of the point where the graph of xy = 8 and  $y = x^2$  intersect is \_\_\_\_\_
- 4.  $\sin\left(2\cos^{-1}(4/5)\right) =$  \_\_\_\_\_
- 5. Which platonic solid has sides shaped like pentagons? a. dodecahedron b. icosahedron c. octahedron d. tetrahedron
- 6. What is the smallest degree possible for a polynomial with integer coefficients that has 5/2 and 3 + 2i as roots ?
- The million-dollar Millennium Problem that has been solved was named for
  a. David Hilbert
  b. William Hodge
  c. Henri Poincaré
  d. Bernhard Riemann
- 8. Find the sum of the following finite sequence, the alternating sum of the first 2,014 positive integers: 1 2 + 3 4 + ... + 2013 2014.
- 9. How many odd numbers between 100 and 999 have three distinct digits?
- 10. What is the greatest common factor (greatest common divisor) of the 66<sup>th</sup> term and the 300<sup>th</sup> term of the Fibonacci sequence (1, 1, 2, 3, 5, ...)?

Return completed test(s) to Mike Breen (email: paoffice@ams.org; fax: 401-331-3842; or mail: c/o American Mathematical Society; 201 Charles St.; Providence, RI 02904)