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We define the *bounded jump*, a jump operator on the bounded Turing (*bT*) degrees (also known as the weak truth-table degrees). We let  $A^{nb}$  denote the  $n$ -th bounded jump of a set  $A$ . We demonstrate several properties of the bounded jump, including that it is strictly increasing and order preserving on the bounded Turing (*bT*) degrees. We show that the bounded jump is related to the Ershov hierarchy. Indeed, for  $n \geq 2$  we have  $X \leq_{bT} \emptyset^{nb} \iff X$  is  $\omega^n$ -c.e.  $\iff X \leq_1 \emptyset^{nb}$ , extending the classical result that  $X \leq_{bT} \emptyset' \iff X$  is  $\omega$ -c.e.. Finally, we prove that the analogue of Shoenfield inversion holds for the bounded jump on the bounded Turing degrees. That is, for every  $X$  such that  $\emptyset^b \leq_{bT} X \leq_{bT} \emptyset^{2b}$ , there is a  $Y \leq_{bT} \emptyset^b$  such that  $Y^b \equiv_{bT} X$ . (Received September 10, 2010)