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The game coloring number $\text{gcol}(G)$ of a graph G is the least k such that if two players take turns choosing the vertices of a graph then either of them can insure that every vertex has less than k neighbors chosen before it, regardless of what choices the other player makes. Clearly $\text{gcol}(G) \leq \Delta(G) + 1$. Sauer and Spencer proved that if two graphs G_1 and G_2 on n vertices satisfy $2\Delta(G_1)\Delta(G_2) < n$ then they pack, i.e., there is an embedding of G_1 into the complement of G_2 . We improve this by showing that if $(\text{gcol}(G_1) - 1)\Delta(G_2) + (\text{gcol}(G_2) - 1)\Delta(G_1) < n$ then G_1 and G_2 pack. To our knowledge this is the first application of such coloring games to a non-game problem. (Received February 03, 2009)