

# BULLETIN

of the

(NEW SERIES)

AMERICAN MATHEMATICAL SOCIETY

### Editors

Articles

Susan Friedlander *Chief Editor* 

Book Reviews

Peter Kuchment

**VOLUME 52** 

NUMBER 3

JULY 2015

Available electronically at www.ams.org/bull/

#### Bulletin (New Series) of the American Mathematical Society

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Subscription information. Bulletin (New Series) of the American Mathematical Society is published quarterly. It is available electronically from www.ams.org/journals/. For paper delivery, subscription prices for Volume 52 (2015) are US\$555 list, US\$444 institutional member, US\$333 individual member, US\$499.50 corporate member. The subscription price for members is included in the annual dues. Subscription renewals are subject to late fees. See www.ams.org/journal-faq for more journal subscription information. If ordering the paper version, add US\$5 for delivery within the United States; US\$8 for delivery outside the United States.

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Bulletin (New Series) of the American Mathematical Society (ISSN 0273-0979 (print); ISSN 1088-9485 (online)) is published quarterly by the American Mathematical Society at 201 Charles Street, Providence, RI 02904-2294 USA. Periodicals postage is paid at Providence, Rhode Island, and additional mailing offices. POSTMASTER: Send address changes to Bulletin (New Series) of the American Mathematical Society, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA.

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## BULLETIN OF THE AMERICAN MATHEMATICAL SOCIETY CONTENTS

Vol. 52, No. 3 July 2	2015
ARTICLES	
Harald A. Helfgott, Growth in groups: ideas and perspectives	357
Ivan Smith, A symplectic prolegomenon	415
Richard Foote, Hy Ginsberg, and V. Kumar Murty, Heilbronn characters	465
MATHEMATICAL PERSPECTIVES	
Gerald L. Alexanderson and Leonard F. Klosinski, About the cover:	
Gaspar Schott's Cursus Mathematicus	497
Selected Mathematical Reviews	503
BOOK REVIEWS	
Gerald R. North (Reviewer), Mathematics & climate, by Hans Kaper and Hans Engler	515
Peter Kuchment (Reviewer), Climate modeling for scientists and engineers,	
by John B. Drake	519
Alexandru Oancea (Reviewer), From Stein to Weinstein and back.  Symplectic geometry of affine complex manifolds, by Kai Cieliebak	
and Yakov Eliashberg	521
Olympia Hadjiliadis (Reviewer), Contract theory in continuous-time	J_1
models, by Jakša Cvitanić and Jianfeng Zhang	531
Sergio Simonella and Herbert Spohn (Reviewers), From Newton	
to Boltzmann: hard spheres and short-range potentials, by Isabelle	
Gallagher, Laure Saint-Raymond, and Benjamin Texier	533
Bo'az Klartag (Reviewer), Geometry of isotropic convex bodies,	
by Silouanos Brazitikos, Apostolos Giannopoulos, Petros Valettas,	<b>F</b> 00
and Beatrice-Helen Vritsiou	539

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## BULLETIN OF THE AMERICAN MATHEMATICAL SOCIETY CONTENTS

Vol. 52, No. 3 July 2	015
ARTICLES	
Harald A. Helfgott, Growth in groups: ideas and perspectives  Ivan Smith, A symplectic prolegomenon	357 415
Richard Foote, Hy Ginsberg, and V. Kumar Murty, Heilbronn characters	465
MATHEMATICAL PERSPECTIVES	
Gerald L. Alexanderson and Leonard F. Klosinski, About the cover: Gaspar Schott's Cursus Mathematicus	497
Selected Mathematical Reviews	503
BOOK REVIEWS	
Gerald R. North (Reviewer), Mathematics & climate, by Hans Kaper and Hans Engler	515
by John B. Drake	519
Symplectic geometry of affine complex manifolds, by Kai Cieliebak and Yakov Eliashberg	521
models, by Jakša Cvitanić and Jianfeng Zhang	531
Sergio Simonella and Herbert Spohn (Reviewers), From Newton to Boltzmann: hard spheres and short-range potentials, by Isabelle	533
Gallagher, Laure Saint-Raymond, and Benjamin Texier	บอย
and Beatrice-Helen Vritsiou	539

