

1st Duke 22

You must have some whites of Eggs; according to the quantity of Lute you will make, and with a brush of rods beat them, till they come all to froth, which must settle to a very clear water. Take one ounce of that water, $\frac{1}{4}$ of an ounce of that light

BULLETIN

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them with the water of the new whites of Eggs. Strain it all through a Sift or fine linen. You must have some pieces of linnen of the bigness of the subjects you will be writing on. Cut them into squares, and settle them to your vessels, and let this lute dry. After which you must compose another lute to put over that. Take some clay 1 part, of Bolus armenic $\frac{1}{4}$, of Sanguis Draconis $\frac{1}{8}$, of quick lime $\frac{1}{2}$ Grind it all to a very subtle powder, and mix exactly $\frac{1}{2}$ part of these things with the half as much of your water of whites of Eggs, and the half as much of hot blood of an hegoat or a sheep as will weigh 1 ounce. Then let you add as much lute to it as you look for the use of the Bolus. But before you mingle these things you must pulverate apart all the matters very subtle, then work it all with your whites of Eggs and your blood very long like dough. This lute is for the back, or breast, of retorts, and for sublimatorys and stills. But for the stills you must make the lute half as much again. Let it be used in the Balneum Mariae, with a low fire.

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Chief Editor

Book Reviews

Robert L. Devaney

Take some Shells of Eggs, 2 Duke. Grind them to powder, sift them. Take 2 parts of enamell ground to an impalpable powder. Mix them with one part of Egg-shells. Then mix them with some water of the whites of Eggs and make a dough with them. It will be penetrated by no spirits. When it is made you must make haste to use it; otherwise it grows hard, and you must be at the trouble of grinding it again and mixing it with new whites of Eggs. These two lutes ought to be put at the top of one another, the first over the first, and the second thoroughly dry. Now when you use the first lute you may put 2 or 3 cloths before you put the lute, or even put the lute severall times. If that lute was not thorowly dry it would be apt to

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