# CONTEMPORARY MATHEMATICS

644

# Analysis, Complex Geometry, and Mathematical Physics: In Honor of Duong H. Phong

May 7–11, 2013 Columbia University, New York, New York

Paul M. N. Feehan
Jian Song
Ben Weinkove
Richard A. Wentworth
Editors



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A Conference in Honor of Duong H. Phong Columbia University, New York, May 7–11, 2013

### Contents

Preface	ix
Scientific program	xi
List of additional participants	XV
Conference photographs	xxi
Bergman kernel and pluripotential theory ZBIGNIEW BŁOCKI	1
On the convergence of the Sasaki-Ricci flow TRISTAN C. COLLINS and ADAM JACOB	11
The signed mean curvature measure QIUYI DAI, XU-JIA WANG, and BIN ZHOU	23
Topics in two-loop superstring perturbation theory ERIC D'HOKER	33
A rigidity theorem for hypersurfaces in higher dimensional space forms Pengfei Guan and Xi Sisi Shen	61
Continuous approximation of quasiplurisubharmonic functions PHILIPPE EYSSIDIEUX, VINCENT GUEDJ, and AHMED ZERIAHI	67
Discrete holomorphicity and Ising model operator formalism CLÉMENT HONGLER, KALLE KYTÖLÄ, and ALI ZAHABI	79
Stable Higgs bundles and Hermitian-Einstein metrics on non-Kähler manif $_{\rm ADAM}$ Jacob	folds 117
Weak solutions to the complex Monge-Ampère equation on Hermitian mar SŁAWOMIR KOŁODZIEJ and NGUYEN NGOC CUONG	nifolds 141
Uniform asymptotic expansion on Riemann surfaces CHIUNG-JU LIU and ZHIQIN LU	159
Scaling asymptotics of heat kernels of line bundles XIAONAN MA, GEORGE MARINESCU, and STEVE ZELDITCH	175
Parabolic frequency monotonicity and a theorem of Hardy-Pólya-Szegö $$\operatorname{Lei}\operatorname{Ni}$$	203
Topology of Dolbeault cohomology groups Mei-Chi Shaw	211

viii CONTENTS

Uniformly bounded orthonormal sections of positive line bundles on complex manifolds	
Bernard Shiffman	227
Poisson equations, uniformization, and geometrical optics MICHAEL TAYLOR	241
Non-Kähler Calabi-Yau manifolds Valentino Tosatti	261
The point source inverse back-scattering problem RAKESH and GUNTHER UHLMANN	279
Local regularity of the complex Monge-Ampère equation Yu Wang	291
Notes on holomorphic string and superstring theory measures of low genus EDWARD WITTEN	307

### **Preface**

Analysis, Complex Geometry and Mathematical Physics: A Conference in Honor of Duong H. Phong was held at Columbia University, New York, May 7–11, 2013. The conference featured thirty speakers who spoke on a range of topics reflecting the breadth and depth of the research interests of Duong H. Phong on the occasion of his sixtieth birthday. These topics included the complex Monge-Ampère equation, pluripotential theory, geometric partial differential equations, theories of integral operators, integrable systems and perturbative superstring theory. A common thread, familiar from Phong's own work, was the focus on the interplay between the deep tools of analysis and the rich structures of geometry and physics. The speakers, who ranged from rising young mathematicians to the most eminent of senior researchers, spoke about new developments in these fields and Phong's fundamental contributions.

The conference attracted over 200 participants, included many who had travelled from afar together with a strong turnout from the greater New York mathematical community, and their participation and interest contributed in an essential way to the richness of this scientific event.

All speakers were invited to contribute to this conference proceedings volume. As editors, we were delighted by the strong response. We received nineteen excellent articles, encompassing a broad array of topics within analysis, complex geometry and mathematical physics. Together they live up to the extraordinarily high level of the conference talks, making this proceedings a fitting tribute to Duong H. Phong on the occasion of his birthday celebration. All manuscripts were carefully refereed and we take this opportunity to thank the anonymous reviewers for their expertise, timely reports, and effort in ensuring the high quality of this proceedings volume.

We thank our conference co-organizers Igor Krichever and Zhiqin Lu for their invaluable help, and together we acknowledge the generous financial support of the National Science Foundation<sup>1</sup> and the Mathematics Department of Columbia University. We also thank the Columbia University graduate students Tristan Collins, Thomas Nyberg, Daniel Rubin, and Yu Wang and staff member, Mary Young, for their assistance in the administration of the conference. We thank Val Red for creating and managing the website for the conference and are grateful to Peter Woit for related technical assistance. Sara Kerens was the official conference photographer and we appreciate her expertise and the wonderful collection of photographs she took during the event. We express our deepest gratitude to the Mathematics Department Administrator, Terrance Cope, who was single-handedly responsible for arranging many of the conference events, including a superb banquet on the

<sup>&</sup>lt;sup>1</sup>Grant number DMS-1266145

x PREFACE

final night of the conference. Finally, we thank all the speakers for their wonderful contributions and the participants for making the conference such a success.

PAUL M. N. FEEHAN Rutgers, The State University of New Jersey

JIAN SONG Rutgers, The State University of New Jersey

BEN WEINKOVE Northwestern University

RICHARD A. WENTWORTH University of Maryland

December 2014

### Scientific program

### Tuesday morning

EDWARD WITTEN (Institute for Advanced Study)
On the work of Phong and D'Hoker on superstring perturbation theory

IGOR KRICHEVER (Columbia University)

 $\label{thm:continuous} The\ universal\ Whitham\ hierarchy\ and\ geometry\ of\ moduli\ spaces\ of\ curves\ with\ punctures$ 

ERIC D'HOKER (University of California, Los Angeles)
Superstring perturbation theory at two loops

### Tuesday afternoon

Andrei Okounkov (Columbia University)

Quantum groups and quantum cohomology

CLÉMENT HONGLER (Columbia University)

Planar Ising model: discrete and continuous structures

ZHIQIN LU (University of California, Irvine) The essential spectrum of the Laplacian

### Wednesday morning

ELIAS M. STEIN (Princeton University)

The development of some ideas of Phong in the theory of singular integral and pseudo-differential operators

ALLAN GREENLEAF (University of Rochester)

Is there a general theory of Fourier integral operators?

Gunther Uhlmann (University of Washington)
Travel time tomography and boundary rigidity

### Wednesday afternoon

MICHAEL E. TAYLOR (University of North Carolina)

Toeplitz operators on uniformly rectifiable domains

Tien-Cuong Dinh (Université Pierre et Marie Curie)

Positive closed currents and dynamics of Henon maps in higher dimension

TRISTAN C. COLLINS (Columbia University)
The boundary of the Kähler cone

### Thursday morning

Charles Fefferman (Princeton University)
Fitting a smooth function to data

ZBIGNIEW BŁOCKI (Uniwersytet Jagielloński) Hörmander's  $\bar{\partial}$ -estimate, some generalizations and new applications

Jacob Sturm (Rutgers University)
Some applications of the Bergman kernel expansion

### Thursday afternoon

Xu-Jia Wang (Australian National University) Potential theory for nonlinear elliptic equations

VINCENT GUEDJ (Institut de Mathématiques de Toulouse) Regularizing properties of the twisted Kähler-Ricci flow

YU WANG (Columbia University)
Small perturbation solutions of the complex Monge-Ampère equation

### Friday morning

NEIL S. TRUDINGER (Australian National University) Weak continuity of nonlinear operators

Sławomir Kołodziej (Uniwersytet Jagielloński) The complex Hessian equations

Lei Ni (University of California, San Diego) Entropy and Gauss curvature flow

### Friday afternoon

Pengfei Guan (McGill University)

New curvature estimates for Weingarten equations

Ahmed Zeriahi (Institut de Mathématiques de Toulouse)

Convergence of the normalized Kähler-Ricci flow on Fano varieties

Adam Jacob (Harvard University)

Stable Higgs bundles and Hermitian-Einstein metrics on non-Kähler manifolds

### Saturday morning

SHING-TUNG YAU (Harvard University)

On the pseudonorm project towards birational classification of algebraic varieties

VALENTINO TOSATTI (Northwestern University)

The Chern-Ricci flow

STEVE ZELDITCH (Northwestern University)

Complex geometry of Laplace eigenfunctions

### Saturday afternoon

JOSEPH J. KOHN (Princeton University)

Weakly pseudoconvex CR manifolds

Mei-Chi Shaw (University of Notre Dame)

Non-closed range property for the Cauchy-Riemann operator in  $L^2$  on a Stein domain

BERNARD SHIFFMAN (Johns Hopkins University)

Critical points of random sections of holomorphic line bundles

### List of additional participants

Ali Aleyasin

Stony Brook University

Xinliang An

Princeton University

Iris Anshel

Columbia University

Guillaume Bal

Columbia University

Turgay Bayraktar

Johns Hopkins University

Shabnam Beheshti

Rutgers University

Christian Benes

City University of New York

Stephane Benoist Columbia University

Alexander Braverman Brown University

Xiaodong Cao

Cornell University

David Catlin Purdue University

Florin Catrina St. John's University

Sagun Chanillo Rutgers University

Albert Chau

University of British Columbia

Daguang Chen

Tsinghua University

Haojie Chen

University of Minnesota

Qiang Chen

Lehigh University

Xuehua Chen

Johns Hopkins University

Po-Ning Chen

Columbia University

Beomjun Choi

Columbia University

Gokhan Civan

University of Maryland

Xin Cui

Lehigh University

Amalia Culiuc Brown University

Panagiota Daskalopoulos Columbia University

Ved Datar

Rutgers University

Daniela De Silva

Columbia University

Alexander Drewitz Columbia University

Frederick Fong Brown University

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Columbia University

Karen Geng York University

Karsten Gimre

Columbia University

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Hubert Goldschmidt Columbia University

Thomas Graham Treesdale, LLC

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Rutgers University

Xiaotao Guo

Columbia University

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Zheng Huang

City University of New York

Matei Ionita

Columbia University

Hervé Jacquet

Columbia University

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University of Michigan

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University of Michigan

Mikhail Khovanov Columbia University Semin Kim

Brown University

Mark Kim

Courant Institute

Lyudmila Korobenko University of Calgary

Nilay Kumar Columbia College

Mijia Lai

University of Rochester

Peter Landesman

Borough of Manhattan Community

College

Gregory Lawler University of Chicago

Peter Lax

New York University

Nam Le

Columbia University

King Leung Lee

Rutgers University - Newark

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Johns Hopkins University

Song-Ying Li

University of California, Irvine

Chen-Yun Lin

University of Connecticut

Bochen Liu

University of Rochester

Chiu-Chu Melissa Liu Columbia University

Fanghua Lin

New York University

Gang Liu

University of Minnesota

Bingyuan Liu

Washington University

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John Loftin

Rutgers University - Newark McGill University

Christopher Lopez Henry Pinkham
University of California, Irvine Columbia University

Sivuan Lu Camelia Pop

McGill University University of Pennsylvania

Marcello Lucia Eric Potash

City University of New York Northwestern University

Nikita Lvov Lihai Qian

Princeton University Cornell University

Donovan McFeron Cristian Rios

Ramapo College of New Jersey University of Calgary

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Columbia University Columbia University

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Columbia University Columbia University

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Wei Sun

The Ohio State University

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Stony Brook University

Hongtan Sun

Johns Hopkins University

Xiaofeng Sun

Lehigh University

Janet Talvacchia

Swarthmore College

Zhongwei Tang

Beijing Normal University

Hung Tran

Cornell University

Mao-Pei Tsui

University of Toledo

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The Ohio State University

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Rutgers University

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Ye-Kai Wang Columbia University Junqi Wang

Rutgers University

Xiaowei Wang

Rutgers University - Newark

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Columbia University

Michael Weinstein Columbia University

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University of Maryland, College Park

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Borough of Manhattan Community

College

Damin Wu

University of Connecticut

Ming Xiao

Rutgers University

Xiaokui Yang

Northwestern University

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Polytechnic Institute of New York

University

Bo Yang

University of California, San Diego

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Yuan Yuan

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Anton Zeitlin

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Yuan Zhang Indiana University-Purdue University Fort Wayne

Yongsheng Zhang Stony Brook University

Wei Zhang Columbia University

Yifei Zhao Columbia University

Peng Zhou Northwestern University

Fan Zhou Columbia University

Seyed Mohsen Zoalroshd University of South Florida

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Shing-Tung Yau (photo credit: Paul Feehan)

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Ahmed Zeriahi (photo credit: Sara Kerens)

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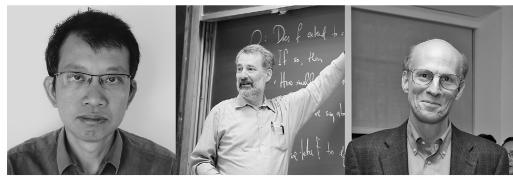
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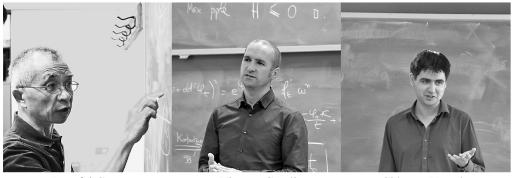
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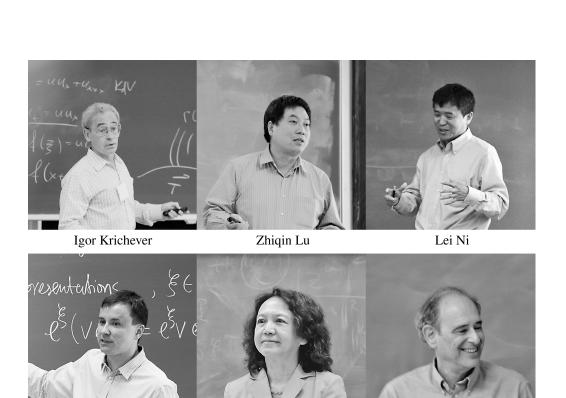
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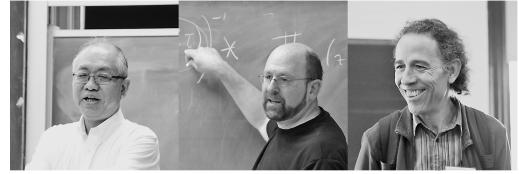
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Xu-Jia Wang

Yu Wang

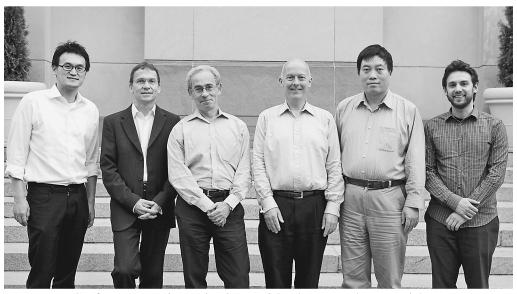
Edward Witten



Shing-Tung Yau

Steve Zelditch

Ahmed Zeriahi



Conference organizers: Jian Song, Richard Wentworth, Igor Krichever, Paul Feehan, Zhiqin Lu and Ben Weinkove



Richard Wentworth, Steve Zelditch and Jacob Sturm



Duong H. Phong and Jian Song



Eric D'Hoker, Duong H. Phong and Edward Witten



Igor Krichever and Andrei Okounkov



Joseph J. Kohn and Shing-Tung Yau



Duong H. Phong



Louis Nirenberg



Elias M. Stein, Regina Y. Liu, Duong H. Phong and Paul Feehan

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- 644 Paul M. N. Feehan, Jian Song, Ben Weinkove, and Richard A. Wentworth, Editors, Analysis, Complex Geometry, and Mathematical Physics, 2015
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This volume contains the proceedings of the Conference on Analysis, Complex Geometry and Mathematical Physics: In Honor of Duong H. Phong, which was held from May 7–11, 2013, at Columbia University, New York. The conference featured thirty speakers who spoke on a range of topics reflecting the breadth and depth of the research interests of Duong H. Phong on the occasion of his sixtieth birthday. A common thread, familiar from Phong's own work, was the focus on the interplay between the deep tools of analysis and the rich structures of geometry and physics.

Papers included in this volume cover topics such as the complex Monge-Ampère equation, pluripotential theory, geometric partial differential equations, theories of integral operators, integrable systems and perturbative superstring theory.

