1172-42-240Jakob Lemvig* (jakle@dtu.dk), Richard Petersens Plads, building 324, 2800 Kgs. Lyngby,
Denmark. On the non-frame property of Gabor systems generated by Hermite
functions. Preliminary report.

Frame set problems in Gabor analysis ask the question for which sampling and modulation rates the corresponding timefrequency shifts of a generating window allow for stable reproducing formulas of L2-functions. In this talk we consider frame sets for Hermite functions, and we show how certain modular characteristics of the Zak transform of Hermite functions play a role in these frame set problems.

It is known that the so-called frame set conjecture is false for Hermite functions of order 4n-2 and 4n-1, where n is a positive integer. We prove that the Gabor frame set conjecture for Hermite functions are also false for all orders of the form 4n and 4n+1, where n is a positive integer. As a conclusion, the frame set conjecture of Hermite functions is false for all order strictly larger than one; the only open case being the Hermite function of order one.

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