1172-42-172Francesco Di Plinio* (francesco.diplinio@wustl.edu), 1 Brookings Dr, St. Louis, MO
63130, and Ioannis Parissis. Maximal Subspace Averages.

We study maximal operators associated to singular averages along finite subsets of the Grassmannian of d-dimensional subspaces of the n-dimensional Euclidean space. The well studied d = 1 case corresponds to the usual directional maximal function. We provide a systematic study of all cases $1 \le d < n$ and prove essentially sharp L^2 bounds for the maximal subspace averaging operator in terms of the cardinality of the finite subset without any assumption on the structure. In the codimension 1 case, that is n = d + 1, we prove the precise critical weak (2, 2)-bound.

Our estimates rely on Fourier analytic almost orthogonality principles, combined with polynomial partitioning, but we also use spatial analysis based on the precise calculation of intersections of d-dimensional plates. (Received August 25, 2021)