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**Jiaxi Nie\*** (jin019@ucsd.edu) and **Jacques Verstraëte** (jbaverstraete@gmail.com). *Ramsey Numbers for Non-trivial Berge Cycles.*

In this paper, we consider an extension of cycle-complete graph Ramsey numbers to Berge cycles in hypergraphs: for  $k \geq 2$ , a *non-trivial Berge  $k$ -cycle* is a family of sets  $e_1, e_2, \dots, e_k$  such that  $e_1 \cap e_2, e_2 \cap e_3, \dots, e_k \cap e_1$  has a system of distinct representatives and  $e_1 \cap e_2 \cap \dots \cap e_k = \emptyset$ . In the case that all the sets  $e_i$  have size three, let  $\mathcal{B}_k$  denotes the family of all non-trivial Berge  $k$ -cycles. The *Ramsey numbers*  $R(t, \mathcal{B}_k)$  denote the minimum  $n$  such that every  $n$ -vertex 3-uniform hypergraph contains either a non-trivial Berge  $k$ -cycle or an independent set of size  $t$ . We prove

$$R(t, \mathcal{B}_{2k}) \leq t^{1 + \frac{1}{2k-1} + \frac{4}{\sqrt{\log t}}}$$

and moreover, we show that if a conjecture of Erdős and Simonovits on girth in graphs is true, then this is tight up to a factor  $t^{o(1)}$  as  $t \rightarrow \infty$ . (Received August 16, 2021)