1171-05-102 Chris Cox* (cocox@iastate.edu) and Ryan Martin. The maximum number of cycles in a planar graph.
For a fixed graph $H$, let $\mathbf{N}_{\mathcal{P}}(n, H)$ denote the maximum number of copies of $H$ in an $n$-vertex planar graph. In this talk, we will focus on the case when $H$ is an even cycle, where it is conjectured that $\mathbf{N}_{\mathcal{P}}\left(n, C_{2 m}\right) \sim(n / m)^{m}$ for all $m \geq 3$. We verify this conjecture for $m \in\{3,4,5,6\}$ and show that $\mathbf{N}_{\mathcal{P}}\left(n, C_{2 m}\right) \lesssim n^{m} / m$ ! for $m \geq 7$. This is accomplished by establishing a connection between this problem and the following question, which is interesting in its own right: which probability mass $\mu$ on the edges of some clique maximizes the probability that $m$ independent samples from $\mu$ form an m-cycle? (Received August 09, 2021)

