Hayan Nam* (nckaplan@math.uci.edu), 4225 Lincoln Swing St, unit 34, Ames, IA 50014, and nathan kaplan. Counting numerical semigroups using polytopes.
A numerical semigroup is an additive monoid that has a finite complement in the set of non-negative integers. For a numerical semigroup $S$, the genus of $S$ is the number of elements in $\mathbb{N} \backslash S$ and the multiplicity is the smallest nonzero element in $S$. In 2008, Bras-Amorós conjectured that the number of numerical semigroups with genus $g$ is increasing as $g$ increases. Later, Kaplan posed a conjecture that implies Bras-Amorós conjecture. In the second half, we prove Kaplan's conjecture when the multiplicity is 4 or 6 by counting the number of integer points in a polytope. Moreover, we find a formula for the number of numerical semigroups with multiplicity 4 and genus $g$. (Received February 16, 2020)

