We consider the following problem. Does there exist an absolute constant $C$ such that for every $n \in N$, every integer $1 \leq k<n$, every origin-symmetric convex body $L$ in $R^{n}$, and every measure $\mu$ with non-negative even continuous density in $R^{n}$,

$$
\mu(L) \leq C^{k} \max _{H \in G r_{n-k}} \mu(L \cap H)|L|^{k / n}
$$

where $G r_{n-k}$ is the Grassmanian of $(n-k)$-dimensional subspaces of $R^{n}$, and $|L|$ stands for volume? This question is an extension to arbitrary measures (in place of volume) and to sections of arbitrary codimension $k$ of the hyperplane conjecture of Bourgain, a major open problem in convex geometry.

We show that the inequality holds for arbitrary origin-symmetric convex bodies, all $k$ and all $\mu$ with $C \sim \sqrt{n}$, and with an absolute constant $C$ for some special classes of bodies. We also prove that for every $\lambda \in(0,1)$ there exists a constant $C=C(\lambda)$ so that the inequality holds for every $n \in N$, every origin-symmetric convex body $L$ in $R^{n}$, every measure $\mu$ with continuous density and the codimension of sections $k \geq \lambda n$. (Received December 19, 2015)

