1120-42-120 John Herr* (jherr@iastate.edu) and Eric Weber (esweber@iastate.edu). Fourier series for singular measures.

Using the Kaczmarz algorithm, we prove that for any singular Borel probability measure μ on [0, 1), every $f \in L^2(\mu)$ possesses a Fourier series of the form $f(x) = \sum_{n=0}^{\infty} c_n e^{2\pi i n x}$. We show that the coefficients c_n can be computed in terms of the quantities $\hat{f}(n) = \int_0^1 f(x) e^{-2\pi i n x} d\mu(x)$. We also demonstrate a Shannon-type sampling theorem for functions that are in a sense μ -bandlimited. (Received February 17, 2016)