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**Louis J. Ratliff** and **David Rush**. *Itoh (e)-valuation rings of an ideal*.

Let  $R$  be a Noetherian ring and  $I$  an  $R$ -ideal. An element  $x$  of  $R$  is integral over  $I$  if there exist  $a_i \in I^i$  for  $i = 1, \dots, n$  such that  $x^n + a_1x^{n-1} + \dots + a_n = 0$ . The set of elements which are integral over  $I$  is the ideal  $\bar{I}$  the integral closure of  $I$ . For ideal  $I$  of positive grade, Rees showed that there exists a unique finite set of Noetherian valuations of  $R$ , now called Rees valuations  $\mathcal{RV}(I)$ , that determines  $\bar{I}$ , i.e.,  $x \in \bar{I}$  iff  $\nu(x) \geq \nu(I)$  for all  $\nu \in \mathcal{RV}(I)$ . Write  $\mathcal{RV}(I) = \{\nu_1, \dots, \nu_n\}$ , and we call  $\nu_1(I), \dots, \nu_n(I)$  the Rees integers of  $I$ .

It is well known that there exists a 1-1 correspondence between  $\mathcal{RV}(I)$  and  $\mathcal{RV}(t^{-1}R[It, t^{-1}])$ , where  $R[It, t^{-1}]$  is the extended Rees algebra of  $I$ . For any positive multiple  $e$  of the Rees integers of  $I$ , Itoh showed that there is a 1-1 correspondence between  $\mathcal{RV}(t^{-1}R[It, t^{-1}])$  and  $\mathcal{RV}(t^{-e}R[It, t^{-e}])$  and that the Rees integers of  $t^{-e}(R[It, t^{-e}])$  are all 1. In this talk, we present a generalization of Itoh's statement. In particular, we show an explicit relationship between the associated valuations rings. (Received February 21, 2016)