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**Antonio Montalbán** and **Richard A. Shore\*** ([shore@math.cornell.edu](mailto:shore@math.cornell.edu)), Department of Mathematics, Malott Hall, Cornell University, Ithaca, NY 14853. *The Limits of Determinacy in Second Order Arithmetic: Consistency and Complexity Strength*. Preliminary report.

We study the consistency and reverse mathematical strength of low levels of determinacy axioms. We derive our results by a recursion/complexity theoretic analysis.

Determinacy for all Boolean combinations of  $F_{\sigma\delta}$  ( $\mathbf{\Pi}_3^0$ ) sets implies the consistency of second-order arithmetic and more. Indeed, it is equivalent to the existence, for every set  $X$  and  $n \in \mathbb{N}$ , of a  $\beta$ -model of  $\mathbf{\Pi}_n^1$ -comprehension containing  $X$ . We prove this by providing a level-by-level analysis of determinacy at the finite level of the difference hierarchy on  $\mathbf{\Pi}_3^0$  sets: For  $n \geq 1$ , determinacy at the  $n$ th level lies strictly between the existence of  $\beta$ -models of  $\mathbf{\Pi}_{n+2}^1$ -comprehension containing any given set  $X$  and of such models of  $\mathbf{\Delta}_{n+2}^1$ -comprehension. Thus it lies strictly between  $\mathbf{\Pi}_{n+2}^1$ -comprehension and  $\mathbf{\Delta}_{n+2}^1$ -comprehension in consistency strength. The major new technical result is a recursion/complexity theoretic one. The  $n$ th determinacy axiom implies closure under the operation taking a set  $X$  to the least  $\Sigma_{n+1}$  admissible containing  $X$  (for  $n = 1$ , this is due to Welch [2012]). (Received February 04, 2013)