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One of the most remarkable results in finite model theory is that for any first order sentence  $\varphi$ ,

$$\lim_{n \rightarrow \infty} \frac{|\{M \models \varphi : |M| = n\}|}{|\{M : |M| = n\}|}$$

is either 0 or 1. In other words, any sentence is realized asymptotically almost surely (a.a.s.) or asymptotically almost never among all finite structures (of a fixed language). This is called the 0-1 law for first order logic. Since its discovery, several other 0-1 laws have been identified for other collections of finite structures, such as finite graphs, finite triangle-free graphs, and finite partial orders.

Given any complete first order theory  $T$ , we can look at the collection of finite subsets of infinite models of  $T$ ,  $\mathcal{C}(T)$ , and ask which sentences hold a.a.s. This gives us a map  $L^{0,1}(\cdot)$  which takes a complete theory and returns the collection of sentences which hold a.a.s. of structures in  $\mathcal{C}(T)$ . We can then ask “How computable can the output  $L^{0,1}(T)$  be, when the input  $T$  is a computable complete theory and  $\mathcal{C}(T)$  satisfies a 0-1 law?”

In this talk we will formalize these concepts and provide a complete answer to this question. (Received February 07, 2013)