1054-14-129Mark W Gross* (mgross@math.ucsd.edu), UCSD Mathematics, 9500 Gilman Drive, La Jolla,
CA 92093-0112, and Rahul Pandharipande and Bernd Siebert. The Tropical Vertex.

Elements of the tropical vertex group, introduced by Kontsevich and Soibelman, are formal families of symplectomorphisms of the 2-dimensional algebraic torus. We prove ordered product factorizations in the tropical vertex group are equivalent to calculations of certain genus 0 relative Gromov-Witten invariants of toric surfaces. The relative invariants which arise have full tangency to a toric divisor at a single unspecified point. The method uses scattering diagrams, tropical curve counts, degeneration formulas, and exact multiple cover calculations in orbifold Gromov-Witten theory. (Received September 10, 2009)