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*p-harmonic functions with drift on graphs.*

Consider a connected finite graph  $E$  with set of vertices  $\mathfrak{X}$ . Choose a nonempty subset  $Y \subset \mathfrak{X}$ , not equal to the whole  $\mathfrak{X}$ , and call it the boundary  $Y = \partial\mathfrak{X}$ . We are given a real valued function  $F : Y \rightarrow \mathbb{R}$ . Our objective is to find function  $u$  on  $\mathfrak{X}$ , such that  $u = F$  on  $Y$  and  $u$  satisfies the following equation for all  $x \in \mathfrak{X} \setminus Y$

$$u(x) = \alpha \max_{y \in S(x)} u(y) + \beta \min_{y \in S(x)} u(y) + \gamma \left( \frac{\sum_{y \in S(x)} u(y)}{\#(S(x))} \right),$$

where  $\alpha, \beta$ , and  $\gamma$  are some predetermined non-negative constants such that  $\alpha + \beta + \gamma = 1$ , for  $x \in \mathfrak{X}$ ,  $S(x)$  is the set of vertices connected to  $x$  by an edge, and  $\#(S(x))$  denotes the cardinality of  $S(x)$ . We prove uniqueness and existence of the solution of the above Dirichlet problem and study qualitative studies of the properties of the solutions. (Received December 28, 2009)