1057-17-391 Anthony Giaquinto*, Department of Mathematics, Loyola University Chicago, Chicago, IL 60626, and Murray Gerstenhaber (mgersten@math.upenn. edu), Department of Mathematics, University of Pennsylvania, Philadelphia, PA 19104. Graphs, Frobenius functionals, and the classical Yang-Baxter equation.
A Lie algebra is Frobenius if it admits a linear functional $F$ such that the Kirillov form $F([x, y])$ is non-degenerate. If $g$ is the $m$-th maximal parabolic subalgebra $\mathrm{P}(\mathrm{n}, \mathrm{m})$ of $\mathrm{sl}(\mathrm{n})$ this occurs precisely when $(\mathrm{n}, \mathrm{m})=1$. We define a "cyclic" functional F on $\mathrm{P}(\mathrm{n}, \mathrm{m})$ and prove it is non-degenerate using properties of certain graphs associated to F . These graphs also provide in some cases readily computable associated solutions of the classical Yang-Baxter equation. Such solutions produce non-commutative versions of the associated parabolic group. (Received January 26, 2010)

