Svitlana Mayboroda*, svitlana@math.purdue.edu, and Alexander Volberg. Square function, Riesz transform and rectifiability.

A celebrated 1991 theorem of David and Semmes ascertains that the L^2 -boundedness of all Calderón-Zygmund operators with respect to a Hausdorff measure H^s on a set E implies that s is an integer and E is rectifiable ("contains big pieces of Lipschitz graphs"). In the present work we establish that it is, in fact, sufficient to assume pointwise boundedness of a single operator, namely, the square function associated to the Riesz transform, in order to arrive to the same conclusion. (Received September 09, 2009)