local homomorphism.
In studying direct-sum behavior of finitely generated modules over a local ring ( $R, \mathfrak{m}, k$ ), it is often useful to pass to a larger local ring via a flat local homomorphism $R \rightarrow S$. For example, $S$ might be the completion or the Henselization of $R$; or $S$ might be obtained by lifting the map $k \rightarrow \bar{k}$, where $\bar{k}$ is the algebraic closure of $k$. One then needs to understand how the category of $R$-modules sits inside the corresponding category of $S$-modules. In particular, one needs to know which $S$-modules actually come from $R$-modules (that is, are in the image of the functor $M \mapsto S \otimes_{R} M$ ). We will discuss this problem, with particular emphasis on the case of rings of dimension zero or one. (Received September 09, 2009)

