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**A Daniilidis, J Malick, A Lewis and H Sendov\*** (hssendov@stats.uwo.ca), The University of Western Ontario, Western Science Centre - Room 262, Dept. of Statistical & Actuarial Sciences, London, Ontario N6A 5B7, Canada. *Spectral Manifolds*.

It is well known that the set of all  $n \times n$  symmetric matrices of rank  $k$  is a smooth manifold. This set can be described as those symmetric matrices whose ordered vector of eigenvalues has exactly  $n - k$  zeros. The set of all vectors in  $\mathcal{R}^n$  with exactly  $n - k$  zero entries is itself an analytic manifold.

In this work, we characterize the manifolds  $M$  in  $\mathcal{R}^n$  with the property that the set of all  $n \times n$  symmetric matrices whose ordered vector of eigenvalues belongs to  $M$  is a manifold. In particular, we show that if  $M$  is a  $C^2$ ,  $C^\infty$ , or  $C^\omega$  manifold then so is the corresponding matrix set. We give a formula for the dimension of the matrix manifold in terms of the dimension of  $M$ .

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