1048-13-303 Michael Freeze\* (freezem@uncw.edu), Department of Mathematics and Statistics, 601 South College Road, Wilmington, NC 28403, and Alfred Geroldinger. Unions of Sets of Lengths.
Let H be an atomic monoid. For k ∈ N let V<sub>k</sub>(H) denote the set of all m ∈ N such that there exist atoms u<sub>1</sub>,..., u<sub>k</sub>, v<sub>1</sub>,..., v<sub>m</sub> ∈ H with u<sub>1</sub>...u<sub>k</sub> = v<sub>1</sub>...v<sub>m</sub>. We consider conditions on H for which V<sub>k</sub>(H) is eventually an arithmetical progression. (Received February 10, 2009)