Let Z be the ring of integers and Q the field of rational numbers. Suppose that T is a ring which contains Z and A is a ring which contains both $Q$ and $T$. Then if $f(X)$ is a polynomial in $Q[X]$ we can consider the element $f(t)$ where $t$ is an element of $T$. We then consider the ring of all polynomials in $Q[X]$ which map $T$ to itself. This ring is well-defined even if T has zero-divisors, or is not commutative. Easy, nontrivial examples can be obtained by letting T be the ring of integral quaternions, the ring of $n$ by $n$ integral matrices, or the ring of integers in a finite algebraic extension of Q . We investigate when such rings are Prufer domains. (Received February 09, 2009)

