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Stephanie B. Alexander* (sba@math.uiuc.edu), Mathematics Department, MC-382, UIUC, 1409 West Green St., Urbana, IL 61801, and Mohammad Ghomi and Jeremy A. Wong. Topology of nonnegatively curved Euclidean hypersurfaces spanning a prescribed boundary. Preliminary report.

We construct a simple closed curve in \mathbb{R}^3 that is differentiable in its arclength parameter, is \mathbb{C}^∞ in the complement of two points, and bounds infinitely many topologically distinct, compact, embedded, positively curved \mathbb{C}^∞ surfaces. In contrast, for a $\mathbb{C}^{1,1}$ curve we prove there can be at most finitely many topologically distinct, compact, locally convex immersed spanning surfaces. In higher dimensions, we prove that a smooth, compact, connected submanifold of codimension 2 immersed in \mathbb{R}^{n+1} , n > 2, bounds at most finitely many topologically distinct, positively curved immersed hypersurfaces, complete but not necessarily compact. When n = 2, topological finiteness extends to noncompact positively curved spanning surfaces if they are embedded. (Received August 07, 2007)