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C. Y. Chan and P. Tragoonsirisak* (pxt6365@louisiana.edu), Department of Mathematics, University of Louisiana at Lafayette, Lafayette, LA 70504-1010. Computation of the critical coefficient in a multi-dimensional quenching problem with a logarithmic singularity in \mathbb{R}^N .

We study the following multi-dimensional semilinear parabolic first initial-boundary value problem,

$$u_t - \Delta u = \alpha \left(1 + |x|\right)^m \left(-\frac{\ln\left(1 - u\right)}{u}\right) \text{ in } \mathbb{R}^N \times (0, T],$$
$$u\left(x, 0\right) = 0 \text{ for } x \in \mathbb{R}^N, \ u\left(x, t\right) \to 0 \text{ as } |x| \to \infty \text{ for } 0 < t \le T,$$

where α , m and T are real numbers such that $\alpha > 0$ and T > 0. For $N \ge 3$ and m < -2, it is shown that there exists a unique critical coefficient α^* such that u exists globally for $\alpha < \alpha^*$ and quenches in a finite time for $\alpha > \alpha^*$. A computational method for finding α^* is devised. (Received January 23, 2008)