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Hongqiu Chen* (hchen1@memphis.edu), Department of Mathematical Sciences, University of Memphis, Memphis, TN 38152, and **Jerry L Bona**. *Sharp Results of Well-posedness*.

Consider the initial-value problem

$$(**) \quad \left. \begin{aligned} u_t + u_x + g(u)_x + Lu_t &= 0, & x \in \mathbb{R}, \quad t > 0, \\ u(x, 0) &= u_0(x), & x \in \mathbb{R}, \end{aligned} \right\}$$

where $u = u(x, t)$ is a real-valued function, L is a Fourier multiplier operator with real symbol $\alpha(\xi)$, that is $\widehat{Lv}(\xi) = \alpha(\xi)\widehat{v}(\xi)$, and g is a smooth, real-valued function of a real variable. Equations of this form arise as models of wave propagation in a variety of physical contexts. Here, fundamental issues of local and global well-posedness are established for L_p , H^s and bore-like or kink-like initial data. In the special case where $\alpha(\xi) = |\xi|^r$ wherein $r > 1$ and $g(u) = \frac{1}{2}u^2$, the initial value problem (**) is locally well-posed in H^s if r and s satisfy one of the following three conditions:

- (a) $r \geq 1$ and $s > \frac{1}{2}$;
- (b) $r > \frac{5}{4}$ and $s > \frac{1}{4}$;
- (c) $r > \frac{3}{2}$ and $s \geq 0$.

In addition, if $r > 1$ and $s \geq 1 - \frac{r}{2}$, then the well-posedness is global. (Received February 04, 2008)