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Iain Gordon, Emil Horozov and Milen Yakimov^{*} (yakimov@math.ucsb.edu), Dept. Mathematics, University of California, Santa Barbara, CA 93106. The real loci of Calogero-Moser spaces, representations of rational Cherednik algebras, and the Shapiro Conjecture.

We will describe a criterion for the reality of irreducible representations of the rational Cherednik algebras $H_{0,1}(S_n)$. It will be applied to study the real loci of the Calogero-Moser spaces. As a consequence, we will give a second (independent) proof of the the Shapiro Conjecture for Grassmannians, proved by Mukhin, Tarasov, and Varchenko. (Received January 30, 2008)