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**Malgorzata M Czerwinska\*** (mmczerwi@olemiss.edu), Department of Mathematics, University of Mississippi, University, MS 38677-1848. *Exposed and strongly exposed points in symmetric spaces of measurable operators.*

Let  $\mathcal{M}$  be a semifinite von Neumann algebra with a faithful, normal, semifinite trace  $\tau$ , and  $E$  be a symmetric Banach function space on  $[0, \tau(\mathbf{1}))$ . The symmetric spaces  $E(\mathcal{M}, \tau)$  of  $\tau$ -measurable operators consists of all  $\tau$ -measurable operators  $x$  for which the singular value function  $\mu(x)$  belongs to  $E$  and is equipped with the norm  $\|x\|_{E(\mathcal{M}, \tau)} = \|\mu(x)\|_E$ .

Let  $(X, \|\cdot\|)$  be a Banach space, with the unit sphere and the unit ball denoted by  $S_X$  and  $B_X$ , respectively. An element  $x \in S_X$  is an *exposed point* of  $B_X$  if there exists a normalized functional  $F \in X^*$  which supports  $B_X$  exactly at  $x$ , i.e.  $F(x) = 1$  and  $F(y) \neq 1$  for every  $y \in B_X \setminus \{x\}$ . If, moreover,  $F(x_n) \rightarrow 1$  implies  $\|x - x_n\| \rightarrow 0$  for all sequences  $\{x_n\} \subset B_X$ , then  $x$  is a *strongly exposed point* of  $B_X$  and  $F$  *strongly exposes*  $B_X$  at  $x$ .

We will discuss the relationships between exposed and strongly exposed points of the unit ball of an order continuous symmetric function space  $E$ , and of the unit ball of the space of  $\tau$ -measurable operators  $E(\mathcal{M}, \tau)$ . It is a joint work with Anna Kamińska and Damian Kubiak from the University of Memphis. (Received September 22, 2011)