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MC 0112, La Jolla, CA 92093. *Necessary Spectral Conditions for 2-coloring Regular 3-uniform  
Hypergraphs.*

Hoffman proved that for a simple graph  $G$ , the chromatic number,  $\chi(G)$ , obeys  $\chi(G) \leq 1 - \frac{\lambda_1}{\lambda_n}$  where  $\lambda_1$  and  $\lambda_n$  are the maximal and minimal eigenvalues of the adjacency matrix of  $G$  respectively. Lovász later showed that  $\chi(G) \leq 1 - \frac{\lambda_1}{\lambda_n}$  for any (perhaps negatively) weighted adjacency matrix.

We give a short probabilistic proof of Lovász's theorem. We then extend the technique to derive generalizations of Hoffman's theorem for regular graphs regarding colorings allowing a certain proportion of edge-conflicts. Finally, we derive our main result: If a  $d$ -regular 3-uniform hypergraph is 2-colorable, then  $-\lambda_{min} \geq \frac{2d}{3}$  where  $\lambda_{min}$  is the smallest eigenvalue of an appropriately-weighted adjacency matrix for the underlying graph. (Received September 23, 2011)