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**Marcus J Pivato\*** (marcuspivato@gmail.com), Department of Mathematics, Trent University, 1600 West Bank Drive, Peterborough, Ontario K9J 7B8, Canada. *Variable-population voting rules.*

Let  $X$  be a set of social alternatives. Let  $V$  be a set of ‘signals’. A *variable population voting rule*  $F$  takes any number of anonymous votes drawn from  $V$  as input, and produces a nonempty subset of  $X$  as output. For example, let  $R$  be a linearly ordered abelian group (e.g.  $\mathbb{R}$ ). In an  *$R$ -valued scoring rule*, each vote in  $V$  assigns an  $R$ -valued ‘score’ to each alternative in  $X$ . We add up the scores of each alternative over all votes in the profile, and select the alternative(s) with the highest aggregate score. An  *$R$ -valued balance rule* is similar, but now an  $R$ -valued scoring rule is used to decide each two-way race; we select the alternative(s) which beat or tie every other alternative.  $F$  satisfies *reinforcement* if, whenever two disjoint sets of voters each select some subset  $Y \subseteq X$ , the union of these two sets will also select  $Y$ . We show that  $F$  satisfies reinforcement iff  $F$  is a balance rule. If  $F$  satisfies a form of neutrality, then  $F$  satisfies reinforcement iff  $F$  is a scoring rule; this generalizes a result of Myerson (1995). We discuss the uniqueness of these representations. Finally, we axiomatically characterize two scoring rules: *formally utilitarian* voting and *range voting*. (Received July 28, 2011)