1077-57-240 Heather M. Russell* (heathemr@usc.edu), Julianna S. Tymoczko and Matthew Housley. Interactions between knot theory and representations of the symmetric group.

Springer varieties are a special collection of flag varieties whose homology carries an action of the symmetric group with the top-dimensional homology an irreducible representation. For a fixed integer n, there is a Springer variety for each partition of n. In the case of two-element partitions, Springer varieties have important connections to Khovanov's theory of categorified tangle invariants. In past work, we use this to explicitly construct the Springer representation for two-element partitions of n. This construction operates skein-theoretically on crossingless matchings.

This simple, knot-theoretic approach can be used once again to construct the Springer representation in the case of three-element partitions of n. In this setting embedded, trivalent, directed graphs called sl(3) webs replace crossingless matchings, and the skein relation is more interesting. We will show how certain combinatorial data about symmetric group representations are naturally and intuitively encoded in this knot-theoretic framework. (Received August 16, 2011)