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*The Segal conjecture in homotopical group theory.* Preliminary report.

For a finite  $p$ -group  $P$  and a finite group  $G$ , the Segal conjecture implies a description, due to Lewis–May–McClure, of the spectrum of stable maps from  $BP$  to the  $p$ -completion of  $BG$  as a wedge sum of suspension spectra. In unpublished work, Lannes showed that when  $P$  has order  $p$ , one can replace  $BG$  with a space  $X$  that shares some homotopy characteristics with the classifying space of a finite group, and obtain a similar description. We will discuss this work and show how, using iterated homotopy fixed points, one can obtain a description of the spectrum of stable maps from  $BP$  to  $X$  for a general finite  $p$ -group  $P$ . The allowable spaces  $X$  in this setting include  $p$ -compact groups and  $p$ -local finite groups, and thus we obtain a version of the Segal conjecture for those spaces. (Received September 21, 2011)