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**Quanlei Fang\***, quanlei.fang@bcc.cuny.edu, and **Jingbo Xia**. *Essential normality of polynomial-generated submodules.*

Recently, Douglas and Wang proved that for each polynomial  $q$ , the submodule  $[q]$  of the Bergman module on the ball generated by  $q$  is essentially normal. Using improved techniques, we show that the analogue of this result holds in the case of the Hardy space  $H^2(S)$  and in the first non-trivial case  $H_2^2$  of free Hilbert module over  $\mathbf{C}[z_1, z_2]$ , and more. More specifically, we consider the family of reproducing-kernel Hilbert spaces  $\mathcal{H}^{(t)}$ ,  $-n \leq t < \infty$ , where  $n$  is the complex dimension of the ball. Here,  $\mathcal{H}^{(t)}$  is defined by the reproducing kernel  $(1 - \langle \zeta, z \rangle)^{-n-1-t}$ , and one can think of the value  $t$  as the “weight” for the space  $\mathcal{H}^{(t)}$ . We show that if  $q \in \mathbf{C}[z_1, \dots, z_n]$ , then for each real value  $-3 < t < \infty$  the submodule  $[q]^{(t)}$  of  $\mathcal{H}^{(t)}$  is  $p$ -essentially normal for every  $p > n$ . Applications of this general result to the cases  $t = -1$  and  $t = -2$  yield the above-mentioned results for  $H^2(S)$  and  $H_2^2$  respectively. (Received September 04, 2011)