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**Kevin Rion\*** ([krion@bridgew.edu](mailto:krion@bridgew.edu)), Mathematics and Computer Science Department,  
Bridgewater State University, Bridgewater, MA 02325. *The Aluthge Sequence of a Shift Operator.*

For any bounded linear operator  $T$  on a Hilbert space, the Aluthge transform is defined by  $\Delta(T) = |T|^{\frac{1}{2}} U |T|^{\frac{1}{2}}$ , where  $T = U |T|$  is the polar decomposition of  $T$ . Moreover, the  $n$ th Aluthge transform is defined for  $n \geq 1$  by  $\Delta^n(T) = \Delta(\Delta^{n-1}(T))$ , with  $\Delta^0(T) = T$ . If  $T$  is a bilateral forward shift, the Aluthge transform is also a bilateral forward shift with weights easily described as a function of the weights of  $T$ . We modify this description so that the successive operators  $T, \Delta(T), \Delta^2(T), \dots$  are seen as resulting from an elementary looking averaging process. We then use a strong form of Stirling's formula and Chebyshev's inequality to draw some conclusions about the convergence or divergence of the sequence  $T, \Delta(T), \Delta^2(T), \dots$ . (Received September 21, 2011)