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**Faruk F. Abi-Khuzam\*** (farukakh@aub.edu.lb), Department of Mathematics, American University of Beirut, Beirut, Lebanon. *On the WAT conjecture on the Torus.*

Let  $f \in L^\infty(T^d)$  with  $\|f\|_{L^\infty(T^d)} \leq 1$ ,  $\nu \in \mathbb{Z}^d$ ,  $n, k \in \mathbb{Z}$  and put  $b_{n,n-k} = \int_E f(x)^n e^{-2\pi i(n-k)\nu \cdot x} dx$ ,  $E = \{x \in T^d : |f(x)| = 1\}$ . Shayya conjectured that, if  $\hat{f}(\xi) = 0$  for all  $\xi$  in a half-space  $S$  of lattice points, and  $\nu \in -S$ , and  $\hat{f}(0) \neq 0$ , then  $\lim_{n \rightarrow \infty} b_{n,n-k} = 0$ ,  $k \in \mathbb{Z}$ . This is a higher dimensional version of an earlier conjecture of Nazarov and Shapiro, the truth of which would imply that any composition operator is weakly asymptotically Toeplitz on the Hardy space  $H^2$ . For  $k = 0$ , Shayya proved that the arithmetic means of  $\{b_{n,n}\}$  decay like  $\{\log N\}^{-1}$ . We prove that the arithmetic means of  $\{b_{n,n-k}\}$  decay like  $\{\log N \log \log N\}^{-1}$  uniformly in  $k \in \mathbb{Z}$ . (Received September 19, 2011)