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**Nobuhiro Asai\*** (nasai@aecc.aichi-edu.ac.jp), 1, Hirosawa, Igaya, Kariya, Aichi, 448-8542, Japan. *MRM triples associated with Brenke type generating functions*. Preliminary report.

In this talk, we will treat the following classical problem:

“Determine all possible orthogonal polynomials generated by Brenke type generating functions,

$$\psi(t, x) := B(t)h(tx) = \sum_{n=0}^{\infty} h_n P_n(x)t^n, \quad (1)$$

where functions  $h(x)$  and  $B(t)$  are analytic around the origin,

$$h(x) = \sum_{n=0}^{\infty} h_n x^n, \quad B(t) = \sum_{n=0}^{\infty} b_n t^n$$

with  $h_n \neq 0$  for  $n \geq 0$  and  $h(0) = B(0) = 1$  just for normalizations”. Chihara ('68 '71) classified them essentially into four classes I–IV. However, explicit expressions of  $\psi(t, x)$  for each class, that is,  $B(t)$  and  $h(t)$ , were not obtained in his papers. Moreover, the associated Jacobi-Szegö parameters for Class IV were not given although several examples were mentioned briefly by a very vague explanation. In this talk, we will report that  $B(t)$  and  $h(t)$  for each class can be expressed by  $q$ -hypergeometric series and the Jacobi-Szegö parameters for Class IV coincide with those of discrete  $q$ -Hermite polynomials. The present results are based on the joint work with I.Kubo (Hiroshima, Japan) and H.-H. Kuo (LSU). (Received September 19, 2011)