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Vitaly Bergelson, Neil Hindman and Kendall Williams* (kendall.williams@usma.edu).

Elements of Tensor Products of Ultrafilters on \mathbb{N} . Preliminary report.

Let $a_1, a_2, \dots, a_m \in \mathbb{Z}$, $a_m > 0$, and $\langle x_n \rangle_{n=1}^\infty$ in \mathbb{N} . A Milliken-Taylor system, $MT(\langle a_i \rangle_{i=1}^m, \langle x_n \rangle_{n=1}^\infty)$, is $\{\sum_{i=1}^m a_i \sum_{t \in F_i} x_t : F_1, F_2, \dots, F_m \text{ are increasing finite nonempty subsets of } \mathbb{N}\}$. Given $\langle x_n \rangle_{n=1}^\infty$ in \mathbb{N} and $A \subseteq \mathbb{N}$, there is a sum subsystem $\langle y_n \rangle_{n=1}^\infty$ of $\langle x_n \rangle_{n=1}^\infty$ such that the finite sums of $\langle x_n \rangle_{n=1}^\infty$ are contained in A if and only if there is an idempotent p in the Stone-Ćech Compactification of \mathbb{N} such that $A \in p$ and for each $m \in \mathbb{N}$, the finite sums of $\langle x_n \rangle_{n=1}^\infty$ are in p . A similar result holds where the finite sums are replaced by the Milliken-Taylor system and A is an element of a sum of ultrafilters. Further generalizations of this result hold wherein the Milliken-Taylor system is replaced by a more general analogous set and A is an element of an arbitrary polynomial evaluated on ultrafilters or it is an element of a tensor product of ultrafilters. (Received September 21, 2011)