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**Lynnelle L Ye\*** ([lynnelle@stanford.edu](mailto:lynnelle@stanford.edu)), 531 Lasuen Mall, P.O. Box 16820, Stanford, CA 94309. *Bounds and Asymptotics for Various Properties of Numerical Semigroups.*

A numerical semigroup  $S$  is a subset of the nonnegative integers  $\mathbb{N}_0$  which contains 0, is closed under addition, and has finite complement in  $\mathbb{N}_0$ . We call the cardinality of  $\mathbb{N}_0 \setminus S$  the genus of  $S$ , or  $g(S)$ , and we call the largest element of  $\mathbb{N}_0 \setminus S$  the Frobenius number of  $S$ , or  $F(S)$ . Let  $N(g)$  be the number of numerical semigroups with genus  $g$  and  $C(F)$  be the number of numerical semigroups with Frobenius number  $F$ . It is known that as  $g$  increases,  $N(g)$  eventually grows at a rate of  $\varphi^g$ . Asymptotics for  $C(F)$  have not previously been computed. Here we show that as  $F$  increases,  $C(F)$  grows at a rate of  $\sqrt{2^F}$ . We also find asymptotics for the proportion of maximal embedding dimension numerical semigroups and the typical number of effective generators of a numerical semigroup as  $g$  increases. Finally, we compute a recurrence for  $N(g)$  which shows that  $N(g) - N(g - 1) \leq N(g + 1)$  for all  $g$ , not just for  $g$  large. (Received September 15, 2011)