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Vladimir, Kosygina st., 2, Moscow, 119334, Russia. Non-abelian quadratic Poisson brackets:
From noncommutative ODE to noncommutative Algebraic Geometry and back. Preliminary report.

We study some general non-abelian quadratic Poisson brackets. The study was motivated by some top-like integrable systems on associative algebras. We give and interpret the compatibility condition of linear and quadratic non-abelian Poisson structures using Hochshild cohomology of infinitesimal associative bialgebras. We give a full classification of such structures in the case of the free associative algebra with 2 generators. Relations with double Poisson structure of M. Van den Bergh and H_0 -structures of W. Crawley-Boevey are discussed. (Received September 20, 2011)