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**Yonatan Harpaz\*** (harpazy@gmail.com) and **Tomer M. Schlank**  
(tomer.schlank@gmail.com). *Homotopy Obstructions to Rational Points - II.*

In 1969 Artin and Mazur defined the étale homotopy type  $\acute{E}t(X)$  of a scheme  $X$  as a way to homotopically realize the étale topos of  $X$ . In this talk we will consider the relative situation  $X \rightarrow S$  and define a relative version  $\acute{E}t/S(X)$  of this notion. We call it the **relative homotopy type of  $X$  over  $S$** .

It turns out that the relative homotopy type can be especially useful in studying the sections of the map  $X \rightarrow S$ . In particular this notion can be used in order to obtain homotopy-theoretic obstructions to the existence of a section.

In the special case where  $S = \text{Spec}(K)$  is the spectrum of a field  $K$ , the set of sections are just the set of  $K$ -rational points  $X(K)$ . In that case the obstructions we obtain are a direct generalization of Grothendieck's section obstruction. If furthermore  $K$  is a **global field** then these obstructions can be used to describe various known arithmetic obstructions, such as the regular and étale Brauer-Manin obstructions. This point of view can be used to show new properties of these obstructions. (Received September 19, 2011)