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A field k is called a C_i field if every form of degree d with coefficients in k having more than d^i variables has a non-trivial zero. C_i theory is a powerful tool in that it provides a sharp bound for the number of variables necessary for an arbitrary form to have a non-trivial zero. Suppose f_1, \dots, f_r are forms in s variables over $k := \mathbb{F}_q(t)$, a C_2 field, of degrees d_1, \dots, d_r , respectively. Using extensive combinatorial techniques and C_i theory, we determine a bound for the number of variables necessary for f_1, \dots, f_r to have a projective l -dimensional rational linear space of simultaneous zeros, namely

$$s > l + \sum_{j=1}^r \sum_{w=1}^{d_j} w^2 \binom{d_j - w + l - 1}{l - 1},$$

which is considerably sharper than the analogous bound for a single odd-degree form over \mathbb{Q} . With this result, we also establish that, given $s > 1 + \sum_{j=1}^r \frac{d_j(d_j + 1)(2d_j + 1)}{6}$, for any $\mathbb{F}_q(t)$ -rational zero $\mathbf{a} = (a_1, \dots, a_s)$, we can find infinitely many s -tuples of monic irreducible polynomials $(\varpi_1, \dots, \varpi_s)$, with ϖ_m not all equal, so that $(a_1\varpi_1, \dots, a_s\varpi_s)$ vanishes f_j for $1 \leq j \leq r$. We also prove more general results for forms over C_i fields. (Received September 22, 2011)