

1077-11-1082

**A Johnston\*** (jannaston@gmail.com), 2003 Smith Ave, Baltimore, MD 21209. *Exponential Hensel Lifting.*

Traditional Hensel lifting finds roots for polynomials modulo  $p^n$  given its roots modulo  $p$ , where  $p$  is a prime integer. In other words, given  $f(x) \in \mathbb{Z}[x]$ ,  $r_1 \in \mathbb{Z}/(p)$  such that  $f(r_1) \equiv 0 \pmod{p}$ , and an integer  $n > 1$ , Hensel lifting finds  $r_n \in \mathbb{Z}/(p^n)$  such that  $f(r_n) \equiv 0 \pmod{p^n}$ .

This talk describes an exponential version of Hensel lifting. It details a method for finding discrete logarithms modulo  $p^n$  given a discrete log modulo  $p$ : Given  $\gamma, \sigma \in \mathbb{Z}$ ,  $a_1 \in \mathbb{Z}/(p-1)$  such that  $\gamma^{a_1} \equiv \sigma \pmod{p}$ , and an integer  $n > 1$ , exponential Hensel lifting returns  $a_n$  such that  $\gamma^{a_n} \equiv \sigma \pmod{p^n}$ . (Received September 16, 2011)