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**Craig Eric Larson\*** (clarson@vcu.edu), **Taylor Short** and **Bethany Turner**. *Towards Vizing's Independence Number Conjecture.*

The *chromatic index*  $\chi'$  of a graph is the minimum number of colors that are required so that incident edges are colored different colors. A graph  $G$  with maximum degree  $\Delta$  is *edge critical* if  $\chi(G - e) = \Delta$  for every edge  $e$ . The independence number  $\alpha$  is the cardinality of a largest set of vertices which are pairwise non-adjacent. Vizing conjectured that  $\alpha \leq \frac{n}{2}$  for edge-critical graphs. Woodall has shown that  $\alpha \leq \frac{3n}{5}$  for these graphs. We discuss improvements on this bound that follow from the Independence Decomposition Theorem: namely that any graph can be decomposed into unique subgraphs  $G[X]$  and  $G[X^c]$  having certain nice properties. It follows immediately from this theorem that  $\alpha \leq \frac{3n}{5}$  for *any* graph where  $|X| \leq \frac{n}{5}$ . Further improvements are possible using the special structure of edge-critical graphs. (Received September 22, 2011)