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**Senmei Yao\*** ([smyao@math.wvu.edu](mailto:smyao@math.wvu.edu)), 320 Armstrong Hall, P.O.Box 6310, Morgantown, WV 26505. *Group Connectivity in Line Graphs.*

Tutte introduced the theory of nowhere zero flows and showed that a plane graph  $G$  has a face  $k$ -coloring if and only if  $G$  has a nowhere zero  $A$ -flow, for any Abelian group  $A$  with  $|A| \geq k$ . In 1992 Jaeger et al extended nowhere zero flows to group connectivity of graphs: given an orientation  $D$  of a graph  $G$ , if for any  $b : V(G) \mapsto A$  with  $\sum_{v \in V(G)} b(v) = 0$ , there always exists a map  $f : E(G) \mapsto A - \{0\}$ , such that at each  $v \in V(G)$ ,

$$\sum_{e = vw \text{ is directed from } v \text{ to } w} f(e) - \sum_{e = uv \text{ is directed from } u \text{ to } v} f(e) = b(v)$$

in  $A$ , then  $G$  is  $A$ -connected. Let  $Z_3$  denote the cyclic group of order 3. Jaeger et al conjectured that every 5-edge-connected graph is  $Z_3$ -connected. We proved the following:

- (i) Every 5-edge-connected graph is  $Z_3$ -connected if and only if every 5-edge-connected line graph is  $Z_3$ -connected.
- (ii) Every 6-edge-connected triangular line graph is  $Z_3$ -connected.
- (iii) Every 7-edge-connected triangular claw-free graph is  $Z_3$ -connected.

In particular, every 6-edge-connected triangular line graph and every 7-edge-connected triangular claw-free graph have a nowhere zero 3-flow. (Received September 21, 2011)