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**Adam H. Berliner\*** (berliner@stolaf.edu), MSCS Dept., 1520 St. Olaf Ave., Northfield, MN 55057, and **Richard A. Brualdi**. *2-Matching covered loopy graphs*. Preliminary report.

A  $\{1, 2\}$ -matching  $M$  of a graph  $G$  is a collection of edges such that each vertex of  $G$  meets at most two edges of  $M$ . A perfect 2-matching of  $G$  is a  $\{1, 2\}$ -matching that is a spanning set consisting of pairwise vertex disjoint edges and odd cycles. For a subset of vertices  $X$ ,  $N(X)$  is the set of vertices of  $G$  adjacent to at least one vertex in  $X$ . A theorem of Tutte asserts that a graph  $G$  has a perfect 2-matching if and only if  $|N(X)| \geq |X|$  for all independent sets of vertices  $X$ . We investigate minimal 2-matching covered graphs, i.e. graphs in which every edge is in some perfect 2-matching and the removal of any edge results in a graph without this property. In particular, we will discuss some classes of minimally 2-matching covered loopy graphs (graphs in which each vertex may contain a loop), where a loop is regarded as a cycle of length one. (Received September 19, 2011)