Clique Number, Chromatic Number, and Ramsey Numbers.
Let $Q(n, c)$ denote the minimum clique number over graphs with $n$ vertices and chromatic number $c$. We investigate the asymptotics of $Q(n, c)$ when $n / c$ is held constant. We show that when $n / c$ is an integer $\alpha, Q(n, c)$ has the same growth order as the inverse function of the Ramsey number $R(\alpha+1, t)$ (as a function of $t$ ). Furthermore, we show that if certain asymptotic properties of the Ramsey numbers hold, then $Q(n, c)$ is in fact asymptotically equivalent to the aforementioned inverse function. We use this fact to deduce that $Q(n,\lceil n / 3\rceil)$ is asymptotically equivalent to the inverse function of $R(4, t)$. (Received September 15, 2011)

