1077-03-246 Lynn C. Scow* (lynn@math.uic.edu). Theories without the independence property.

A first-order theory has the *independence property (IP)* if there is some formula in the language of the theory that defines a random graph relation on tuples from any saturated enough model of the theory. In [Laskowski, 1992], it was shown that a theory fails to have the independence property just in case any uniformly definable class of subsets is a Vapnik-Chervonenkis class. Given a set X, a class of subsets C is a Vapnik-Chervonenkis class if for any finite set $F \subset X$, intersections $C \cap F$ with $C \in C$ give less than the maximal number of subsets of F. We will use very homogeneous sequences indexed by ordered graphs in order to characterize this property. (Received August 16, 2011)